

Thermodynamic Properties of Vanadium¹

P. D. Desai²

This work reviews and discusses the data and information on the various thermodynamic properties of vanadium available through March 1985. These include the heat capacity and enthalpy, enthalpy of melting, vapor pressure, and enthalpy of vaporization. The existing data have been critically evaluated and analyzed, and the recommended values for heat capacity, enthalpy, entropy, and Gibbs energy function covering the temperature range from 1 to 3800 K have been generated. These values are referred to temperatures based on IPTS-1968. The units used for various properties are joules per mole ($\text{J}\cdot\text{mol}^{-1}$). The estimated uncertainties in the heat capacity are $\pm 3\%$ below 15 K, $\pm 10\%$ from 15 to 150 K, $\pm 3\%$ from 150 to 298.15 K, $\pm 2\%$ from 298.15 to 1000 K, $\pm 3\%$ from 1000 to the melting point (2202 K), and $\pm 5\%$ in the liquid region.

KEY WORDS: critical evaluation; data analysis; enthalpy; enthalpy of melting; enthalpy of vaporization; Gibbs energy function; heat capacity; recommended values; vanadium; vapor pressure.

1. INTRODUCTION

The principal objective of this work is to critically evaluate and analyze all the available data and information on the heat capacity, enthalpy, and vapor pressure of vanadium and to generate the recommended values of these and other thermodynamic properties from 1 K to the melting point and above.

The discussion of the thermodynamic properties and the details of data analysis are reported in Section 2. The recommended values cover the temperature range from 1 to 3200 K.

¹ Paper presented at the Ninth Symposium on Thermophysical Properties, June 24–27, 1985, Boulder, Colorado, U.S.A.

² Center for Information and Numerical Data Analysis and Synthesis, Purdue University, 2595 Yeager Road, West Lafayette, Indiana, 47906, U.S.A.

2. THERMODYNAMIC PROPERTIES

2.1. Phases and Structures

Vanadium has a bcc (A2) structure isotypic with W. Its atomic weight is 50.9415. A careful study of the values for the superconducting transition temperature, T_c , reported in the literature reveals that T_c is based on the data of Leupold et al. [1] and of Keesom and Radebaugh [2]. Its melting point of 2202 K selected previously by Hultgren et al. [31] was adopted after converting to IPTS-68. This compares with those reported by Rudy [3] (2202 K) and Margrave [4] (2194 K). This temperature and other thermodynamic properties reported here are based on the IPTS-1968.

Table I. Electronic Specific Heat Coefficient, Debye Temperature, and Superconducting Transition Temperature of Vanadium

| Source | γ ($\text{mJ} \cdot \text{mol}^{-1} \cdot \text{K}^{-2}$) | θ_D (K) | T_c (K) |
|---------------------------|--------------------------------------------------------------------|----------------|---------------|
| Leupold et al. [1] | 9.67 | 397.2 | 5.435 |
| Keesom and Radebaugh [2] | 9.92 | 399 | 5.37 |
| Radebaugh [6] | 9.82 | 382 | 5.379 |
| Corak et al. [7] | 8.996 | 298 | |
| Corak et al. [8] | 9.26 | 338 | |
| Sellers et al. [9] | | 399 | |
| Chernoplekov et al. [10] | 9.80 | 373 | |
| Ishikawa [11] | 9.63 | 423 | 5.52 |
| Cheng et al. [12] | 8.87 | 315 | |
| Shen [13] | 9.64 | | 5.084 |
| | 9.64 | | 5.068 |
| Worley et al. [14] | 8.996 | 308 | |
| | 8.954 | 274 | |
| | 8.828 | 273 | |
| Van Reuth [15] | 9.079 | 247 | 4.69 |
| | 9.247 | 345 | |
| Pan et al. [16] | 9.60 | 314 | |
| Ohlendorf and Wicke [17] | 9.47 | 357 | 5.35 |
| Takahashi et al. [18] | | 366 | |
| Kumagai and Ohtsuka [19] | 10.4 | 411 | |
| Corsan and Cook [20] | 9.45 | 377 | 5.17 |
| Junod et al. [21] | 9.9 | 399 | 5.30 |
| Martin [22] | | 391 | |
| Comsa et al. [23] | 9.9 | | 5.4 |
| Vergara et al. [24] | 8.8 | 382 | 5.37 |
| Radebaugh and Keesom [25] | 9.82 | 382 | 5.379 |
| Recommended value | 9.75 ± 0.30 | 385 ± 5 | 5.4 ± 0.3 |

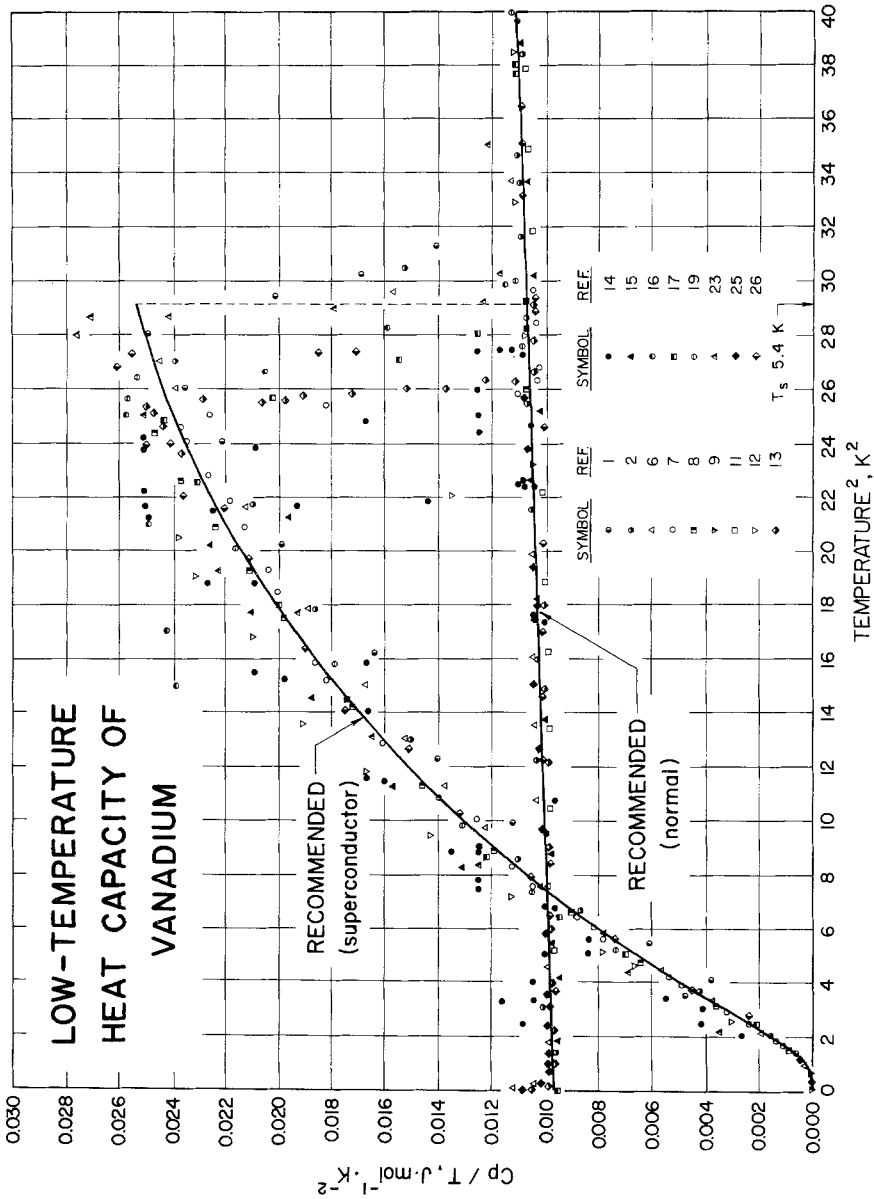


Fig. 1. Very low-temperature (0–40 K) heat capacity of vanadium.

2.2. Low-Temperature Heat Capacity

There have been numerous measurements of the electronic specific heat coefficient, γ , the Debye temperature, θ_D , and the superconducting transition temperature, T_c ; some of them from which the recommended values are derived are listed in Table I. Additionally, Comsa et al. [23] and Vergara et al. [24] reported the data for ultrafine particles, indicating that T_c and γ increase with decreasing particle size.

Table II. Recommended Low-Temperature Heat Capacity of Vanadium

| T (K) | C_p^0 ($J \cdot mol^{-1} \cdot K^{-1}$) | | T (K) | C_p^0 ($J \cdot mol^{-1} \cdot K^{-1}$) |
|------------|------------------------------------------------|----------------------|------------|------------------------------------------------|
| 1 | 0.00024 ^a | 0.00978 ^b | 120 | 16.508 |
| 2 | 0.00992 ^a | 0.0198 ^b | 125 | 17.032 |
| 3 | 0.03573 ^a | 0.0302 ^b | 130 | 17.520 |
| 4 | 0.07448 ^a | 0.0412 ^b | 140 | 18.429 |
| 5 | 0.1196 ^a | 0.0530 ^b | 150 | 19.220 |
| 5.4 | 0.1369 ^a | 0.0580 ^b | 160 | 19.924 |
| 6 | 0.0659 | | 170 | 20.549 |
| 7 | 0.0791 | | 175 | 20.837 |
| 8 | 0.0929 | | 180 | 21.107 |
| 9 | 0.1074 | | 190 | 21.601 |
| 10 | 0.1220 | | 200 | 22.041 |
| 15 | 0.213 | | 210 | 22.438 |
| 20 | 0.360 | | 220 | 22.793 |
| 25 | 0.675 | | 225 | 22.961 |
| 30 | 1.113 | | 230 | 23.121 |
| 40 | 2.348 | | 240 | 23.411 |
| 50 | 4.021 | | 250 | 23.663 |
| 60 | 5.968 | | 260 | 23.882 |
| 70 | 8.105 | | 270 | 24.089 |
| 75 | 9.177 | | 273.15 | 24.155 |
| 80 | 10.250 | | 280 | 24.286 |
| 90 | 12.256 | | 290 | 24.471 |
| 100 | 13.934 | | 298.15 | 24.612 |
| 110 | 15.341 | | | |

$$C_{(\text{electronic})} = \gamma T, \quad \gamma = 9.75 \pm 0.03 \text{ mJ} \cdot \text{mol}^{-1} \cdot \text{K}^{-2}$$

| | Crystal [$V(s)$] | Gas [$V(g)$] |
|--------------------------------------------|-----------------------------------------------------------------------|-------------------------------------------------------------------------|
| $H^0(298.15 \text{ K}) - H^0(0 \text{ K})$ | $4707 \pm 10 \text{ J} \cdot \text{mol}^{-1}$ | $7907 \pm 4 \text{ J} \cdot \text{mol}^{-1}$ |
| $S^0(298.15 \text{ K})$ | $29.708 \pm 0.08 \text{ J} \cdot \text{mol}^{-1} \cdot \text{K}^{-1}$ | $182.189 \pm 0.007 \text{ J} \cdot \text{mol}^{-1} \cdot \text{K}^{-1}$ |

^a Superconductor.

^b Nonsuperconductor in magnetic field.

The recommended C_p^0 values for the normal (nonsuperconducting) state below 5.4 K are calculated from the recommended values for γ and θ_D using the following equation:

$$C_p^0 = \gamma T + [1943.73/\theta_D^3] T^3$$

The recommended C_p^0 values for the superconducting state are based on the data of Leupold et al. [1], Keesom and Radebaugh [2], Corak et al. [7, 8], Kumagai and Ohtsuka [19], and Ohlendorf and Wicke [17]. A comparison of these and other results with the recommended values is shown in Fig. 1.

The recommended C_p^0 values up to 298.15 K are based on the data of Takahashi et al. [27] (-0.8%) and of Anderson [28] ($\pm 2\%$). The data of Ishikawa [11] are up to 20% and those of Bieganski and Stalinski [29] are $\pm 2\%$ above 70 K and considerably lower below 50 K. The data of Takahashi et al. [18] are -1% above 200 K and up to 10% higher below 200 K. The data of Clusius et al. [30] are up to 10% lower and those of Chernoplekov et al. [10] are considerably higher above 10 K and lower below 10 K than the recommended values. It is worth noting that the data of Chernoplekov et al. [10] and those of Takahashi et al. [18] suggest higher C_p^0 values (from 10 to 140 K) than those previously selected by Hultgren et al. [31]. The present recommendations in this temperature range are slightly higher than those recommended by Hultgren et al. [31]. It is thought that more studies are required to corroborate the higher values, especially those of Takahashi et al. [18]. Takahashi et al. [18] observed an anomaly at 220 to 230 K on the electropolished sample which disappeared after annealing at 1000 K. Pan et al. [16] found an anomaly at 195 K evidently connected with a second-order phase transition which may be produced by the ordering of interstitial impurity of hydrogen atoms. The recommended C_p^0 values (Table II) along with the experimental data are shown in Fig. 2. Integration of the recommended C_p^0 and C_p^0/T values yielded $H^0(298.15\text{ K}) - H^0(0\text{ K})$ and $S^0(298.15\text{ K})$ values, listed in Table III along with the values from other sources.

Table III. Room-Temperature Thermodynamic Constants of Vanadium

| Source | $C_p^0(298.15\text{ K})$ ($\text{J} \cdot \text{mol}^{-1} \cdot \text{K}^{-1}$) | $H^0(298.15\text{ K}) - H^0(0\text{ K})$ ($\text{J} \cdot \text{mol}^{-1}$) | $S^0(298.15\text{ K})$ ($\text{J} \cdot \text{mol}^{-1} \cdot \text{K}^{-1}$) |
|----------------------|--------------------------------------------------------------------------------------|----------------------------------------------------------------------------------|------------------------------------------------------------------------------------|
| Present | 24.612 ± 0.15 | 4707 ± 10 | 29.708 ± 0.08 |
| Hultgren et al. [31] | 24.895 | 4640 | 28.911 ± 0.4 |
| Smith [52] | 24.35 ± 0.1 | 4756 ± 50 | 30.89 ± 0.34 |
| Glushko et al. [53] | 24.48 | 4580 | 28.67 |

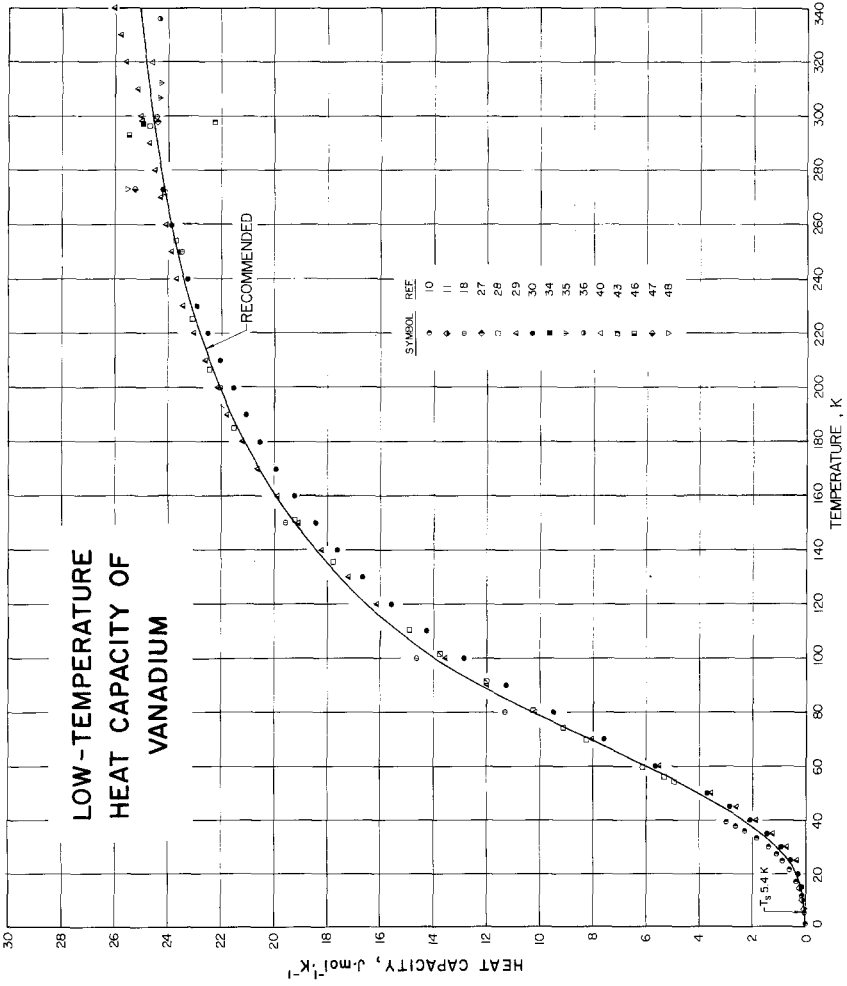


Fig. 2. Low-temperature (0-340 K) heat capacity of vanadium.

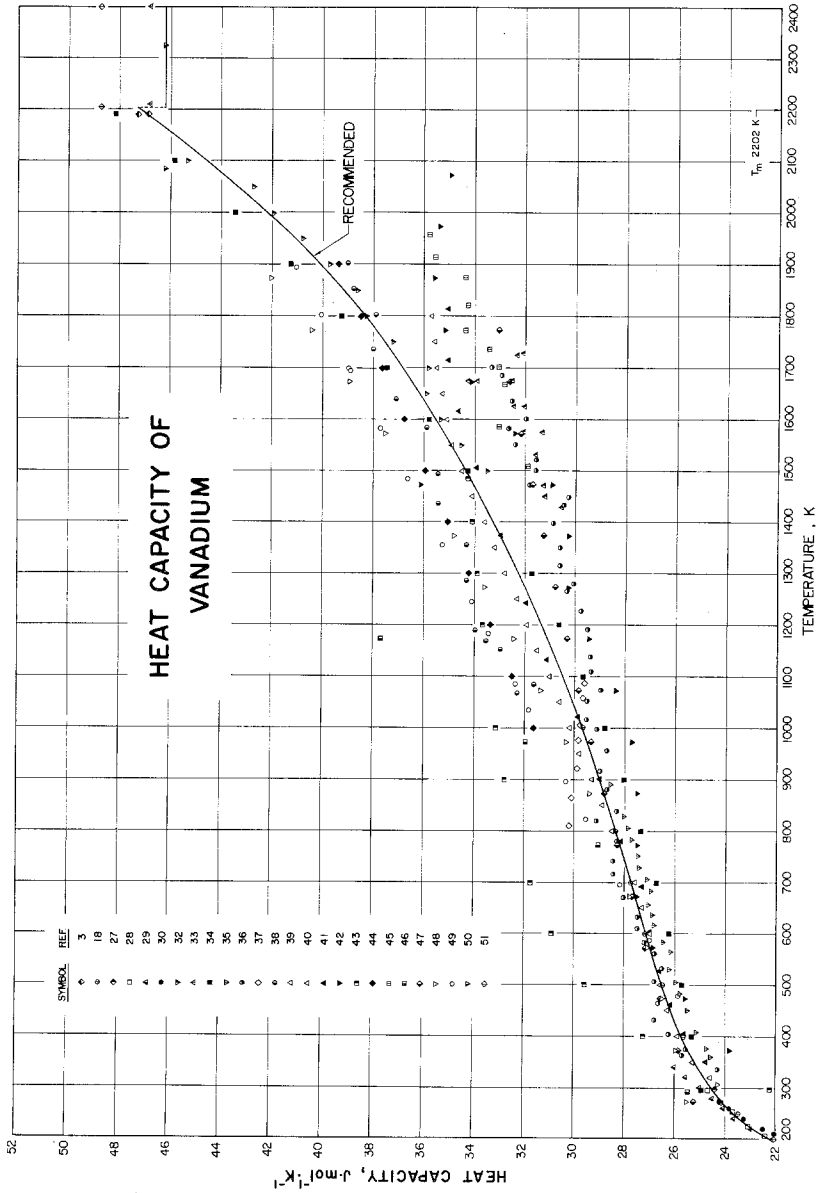


Fig. 3. Heat capacity of vanadium.

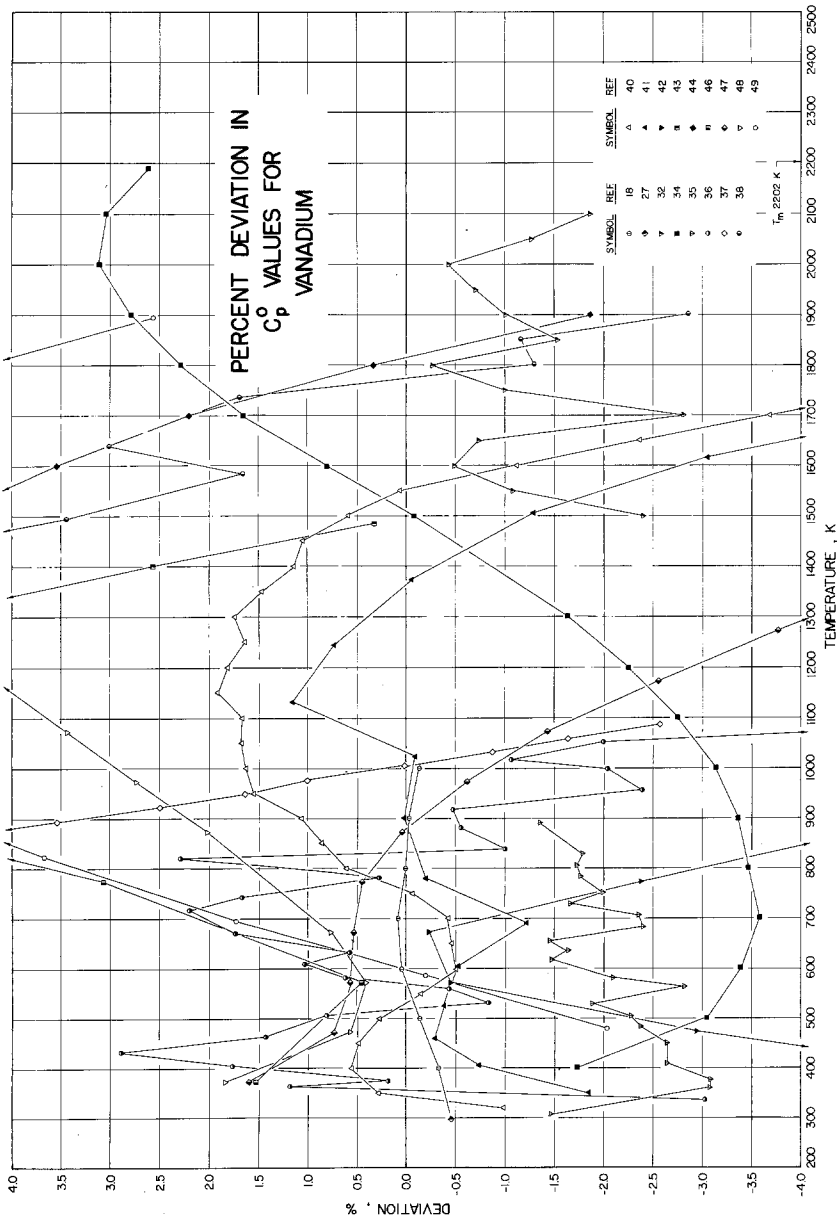


Fig. 4. Percentage deviation in C_p^o values for vanadium.

Table IV. Percentage Deviation in Heat Capacity for Vanadium

| Source | Deviation (%) |
|-----------------------------|------------------------------------------------------------------|
| Bendick and Pepperhoff [36] | ± 3 (<1100 K) Up to -10 (>1100 K) |
| Knezek [37] | ± 3 (>920 K) 6 (<920 K) |
| Arutyunov et al. [38] | ± 3 (>1500 K) 5-8 (<1500 K) |
| Peletskii et al. [39] | Up to -14 |
| Kohlhaas et al. [40] | ± 1 (<900 K) Up to 2 (900-1600 K) Up to -7 (>1600 K) |
| Braun et al. [41] | Up to -2 (<1500 K) Up to -6 (>1500 K) |
| Beakley [42] | Up to -22 |
| Filippov [44] | Up to 6 |
| Filippov et al. [45] | Up to -14 |
| Neimark et al. [46] | Up to 19 |
| Smith [52] | ± 1 (<1200 K) ± 2 (>1200 K) |

2.3. High-Temperature Heat Capacity (Solid)

There have been numerous measurements of the heat capacity of vanadium. The recommended C_p^0 values are based on the data of Takahashi et al. [18] ($\pm 0.5\%$), Cezairliyan et al. [32] ($\pm 2.5\%$), and Chekhovskoi and Kalinkina [35] (-3%). A comparison of other C_p^0 measurements with the recommended values is shown in Table IV. A comparison of enthalpy measurements with the recommended enthalpy values ($y = H^0(T) - H^0(298.15 \text{ K}) / (T - 298.15)$) is shown in Table V.

Table V. Percentage Deviation in Enthalpy for Vanadium

| Source | Deviation (%) |
|-------------------------------|-------------------------------------------|
| Berezin and Chekhovskoi [34] | Up to -3 (<1800 K) ± 1 (>1800 K) |
| Golutvin and Kozlovskaya [43] | Up to 13 |
| Jaeger and Veenstra [47] | Up to 4 (<1173 K) Up to -3 (>1173 K) |
| Jaeger and Veenstra [48] | Up to 4 |
| Fieldhouse and Lang [49] | Up to 6 |

Table VI. Recommended High-Temperature Thermodynamic Properties of Vanadium^a

| T (K) | Condensed phase | | | | | Gas phase V(g) | | | | | | |
|----------|----------------------------------------------------|--------------------------------------------------|--------------------------------------------------|------------------------------------------------------------------------|----------------------------------------------------|--------------------------------------------------|--------------------------------------------------|------------------------------------------------------------------------|----------------------------------------------------|--------------------------------------------------|--------------------------------------------------|------------------------------------------------------------------------|
| | C_p^0 (J·mol ⁻¹ ·K ⁻¹) | $H^0 - H^0(\text{Tr})$ (J·mol ⁻¹) | S^0 (J·mol ⁻¹ ·K ⁻¹) | $-[G^0 - H^0(\text{Tr})]/T$ (J·mol ⁻¹ ·K ⁻¹) | C_p^0 (J·mol ⁻¹ ·K ⁻¹) | $H^0 - H^0(\text{Tr})$ (J·mol ⁻¹) | S^0 (J·mol ⁻¹ ·K ⁻¹) | $-[G^0 - H^0(\text{Tr})]/T$ (J·mol ⁻¹ ·K ⁻¹) | C_p^0 (J·mol ⁻¹ ·K ⁻¹) | $H^0 - H^0(\text{Tr})$ (J·mol ⁻¹) | S^0 (J·mol ⁻¹ ·K ⁻¹) | $-[G^0 - H^0(\text{Tr})]/T$ (J·mol ⁻¹ ·K ⁻¹) |
| 298.15 | 24.612 | 0 | 0.000 | 29.708 | 26.012 | 0 | 0.000 | 182.189 | | | | |
| 300 | 24.641 | 46 | 0.152 | 29.708 | 25.978 | 48 | 0.161 | 182.189 | | | | |
| 400 | 25.783 | 2573 | 7.416 | 30.691 | 24.647 | 2571 | 7.429 | 183.190 | | | | |
| 500 | 26.517 | 5189 | 13.251 | 32.580 | 24.196 | 5007 | 12.867 | 185.042 | | | | |
| 600 | 27.144 | 7873 | 18.143 | 34.729 | 24.283 | 7428 | 17.281 | 187.090 | | | | |
| 700 | 27.736 | 10617 | 22.371 | 36.912 | 24.582 | 9871 | 21.046 | 189.133 | | | | |
| 800 | 28.343 | 13421 | 26.114 | 39.046 | 24.890 | 12345 | 24.349 | 191.107 | | | | |
| 900 | 28.990 | 16287 | 29.489 | 41.101 | 25.116 | 14846 | 27.294 | 192.988 | | | | |
| 1000 | 29.686 | 19221 | 32.579 | 43.067 | 25.237 | 17365 | 29.948 | 194.772 | | | | |
| 1100 | 30.454 | 22227 | 35.444 | 44.946 | 25.262 | 19890 | 32.355 | 196.462 | | | | |
| 1200 | 31.311 | 25315 | 38.130 | 46.743 | 25.214 | 22415 | 34.552 | 198.062 | | | | |
| 1300 | 32.234 | 28491 | 40.673 | 48.464 | 25.117 | 24931 | 36.566 | 199.577 | | | | |
| 1400 | 33.230 | 31764 | 43.097 | 50.117 | 24.994 | 27437 | 38.423 | 201.014 | | | | |
| 1500 | 34.326 | 35141 | 45.427 | 51.708 | 24.864 | 29930 | 40.143 | 202.379 | | | | |
| 1600 | 35.502 | 38632 | 47.679 | 53.243 | 24.739 | 32410 | 41.744 | 203.677 | | | | |
| 1700 | 36.828 | 42247 | 49.871 | 54.728 | 24.630 | 34878 | 43.240 | 204.913 | | | | |
| 1800 | 38.304 | 46002 | 52.017 | 56.168 | 24.545 | 37337 | 44.646 | 206.092 | | | | |
| 1900 | 40.063 | 49916 | 54.133 | 57.569 | 24.487 | 39788 | 45.971 | 207.219 | | | | |
| 2000 | 42.167 | 54027 | 56.241 | 58.935 | 24.460 | 42235 | 47.226 | 208.297 | | | | |
| 2100 | 44.581 | 58362 | 58.355 | 60.272 | 24.467 | 44681 | 48.420 | 209.332 | | | | |

| | | | | | | | | |
|---------|--------|--------|--------|--------|--------|-------|--------|---------|
| 2200 | 47.184 | 62949 | 60.488 | 61.583 | 24.510 | 47130 | 49.559 | 210.325 |
| 2202(s) | 47.238 | 63043 | 60.531 | 61.609 | 24.511 | 47179 | 49.581 | 210.344 |
| 2202(l) | 46.200 | 84043 | 70.068 | 61.609 | 24.511 | 47179 | 49.581 | 210.344 |
| 2300 | 46.200 | 88571 | 72.080 | 63.279 | 24.588 | 49584 | 50.650 | 211.280 |
| 2400 | 46.200 | 93191 | 74.047 | 64.925 | 24.702 | 52049 | 51.698 | 212.200 |
| 2500 | 46.200 | 97811 | 75.933 | 66.516 | 24.853 | 54526 | 52.710 | 213.088 |
| 2600 | 46.200 | 102431 | 77.745 | 68.056 | 25.039 | 57020 | 53.688 | 213.946 |
| 2700 | 46.200 | 107051 | 79.488 | 69.548 | 25.261 | 59535 | 54.637 | 214.776 |
| 2800 | 46.200 | 111671 | 81.168 | 70.994 | 25.517 | 62074 | 55.560 | 215.580 |
| 2900 | 46.200 | 116291 | 82.790 | 72.397 | 25.806 | 64640 | 56.461 | 216.360 |
| 3000 | 46.200 | 120911 | 84.356 | 73.760 | 26.126 | 67236 | 57.341 | 217.118 |
| 3100 | 46.200 | 125531 | 85.871 | 75.085 | 26.476 | 69866 | 58.203 | 217.855 |
| 3200 | 46.200 | 130151 | 87.337 | 76.373 | 26.853 | 72532 | 59.050 | 218.572 |
| 3300 | 46.200 | 134771 | 88.759 | 77.628 | 27.256 | 75237 | 59.882 | 219.272 |
| 3400 | 46.200 | 139391 | 90.138 | 78.849 | 27.682 | 77984 | 60.702 | 219.954 |
| 3500 | 46.200 | 144011 | 91.478 | 80.040 | 28.128 | 80774 | 61.511 | 220.621 |
| 3600 | 46.200 | 148631 | 92.779 | 81.201 | 28.593 | 83610 | 62.310 | 221.273 |
| 3682 | 46.200 | 152419 | 93.819 | 82.131 | 28.986 | 85971 | 62.956 | 221.795 |
| 3700 | 46.200 | 153251 | 94.045 | 82.334 | 29.072 | 86494 | 63.100 | 221.912 |
| 3800 | 46.200 | 157871 | 95.276 | 83.439 | 29.565 | 89425 | 63.881 | 222.537 |

α Enthalpy reference temperature = Tr = 298.15 K. $T_{\text{fus}} = 2202$ K; $\Delta_{\text{fus}}H^0 = 21,000 \pm 2500$ J · mol⁻¹; $\Delta_{\text{fus}}S^0 = 9.537 \pm 1.2$ J · mol⁻¹ · K⁻¹.

Table VII. Values for Enthalpy of Fusion and Heat Capacity of Liquid Vanadium

| Source | $\Delta_{\text{fus}}H^0 (\text{J} \cdot \text{mol}^{-1})$ | $C_p^0 (\text{J} \cdot \text{mol}^{-1} \cdot \text{K}^{-1})$ |
|------------------------------|-----------------------------------------------------------|--------------------------------------------------------------|
| Margrave [4] | | 46.861 47.279 |
| Gathers et al. [5] | 21,905 | |
| Margrave [33] | 18,180 | 46.8 |
| Berezin and Chekhovskoi [34] | 23,037 | |
| Berezin et al. [50] | | 46.191 |
| Treverton and Margrave [51] | 17,305 | 48.744 |
| Smith [52] | 21,500 | 47.43 |

The recommended C_p^0 values along with the experimental data are listed in Table VI and shown in Fig. 3. For the convenience of readers, a systematic plot of the percentage deviation (up to $\pm 4\%$) in C_p^0 values from various measurements is shown in Fig. 4.

2.4. High-Temperature Heat Capacity (Liquid)

The recommended values for the enthalpy of melting, $\Delta_{\text{fus}}H^0 = 21,000 \pm 2500 \text{ J} \cdot \text{mol}^{-1}$ and $C_{p(l)}^0 = 46.200 \pm 2.0 \text{ J} \cdot \text{mol}^{-1} \cdot \text{K}^{-1}$, are based on the data from the reported values given in Table VII.

2.5. Ideal Gas Properties

Thermodynamic quantities for $V(g)$ reported in Table VI are calculated from $C_p^0(g)$ and $S^0(298.15 \text{ K})(g)$ values reported by Chase [54].

Table VIII. Values for Enthalpy of Sublimation of Vanadium at 298.15 K

| Source | $\Delta_{\text{sub}}H^0 (\text{kJ} \cdot \text{mol}^{-1})$ |
|------------------------------------------------------------------------------|------------------------------------------------------------|
| Saxer [55], 1771–1880 K, Knudsen method | 514.53 ± 1.02 |
| Edwards et al. [56], 1666–1882 K, Knudsen method | 513.69 ± 0.61 |
| Moore et al. [57], 1600 K, mass spectrometer–Knudsen method | 501.21 |
| Farber and Srivastava [58], 1900–2412 K, mass spectrometer–Knudsen method | 515.82 ± 1.26 |
| Recommended value | $514.20 (\pm 1.00)$ |

Table IX. Recommended Vapor Pressure of Vanadium, $V_{(s,l)} = V_{(g)}$ ^{a,b}

| T (K) | p (atm) | ΔG^0 (J·mol ⁻¹) | ΔH^0 (J·mol ⁻¹) | p (atm) | T (K) |
|------------|------------------------|----------------------------------------|----------------------------------------|-------------------------------------------------------------------------------------------------------|------------|
| 298.15 | 7.57×10^{-83} | 468,738 | 514,200 | 10^{-10} | 1503 |
| 300 | 2.72×10^{-82} | 468,456 | 514,200 | 10^{-9} | 1593 |
| 400 | 6.58×10^{-60} | 453,200 | 514,198 | 10^{-8} | 1695 |
| 500 | 1.76×10^{-46} | 437,969 | 514,018 | 10^{-7} | 1811 |
| 600 | 1.56×10^{-37} | 422,783 | 513,755 | 10^{-6} | 1945 |
| 700 | 3.81×10^{-31} | 407,645 | 513,454 | 10^{-5} | 2101 |
| 800 | 2.34×10^{-26} | 392,551 | 513,124 | 10^{-4} | 2289 |
| 900 | 1.23×10^{-22} | 377,502 | 512,759 | 10^{-3} | 2522 |
| 1000 | 1.16×10^{-19} | 362,495 | 512,344 | 10^{-2} | 2813 |
| 1200 | 3.32×10^{-15} | 332,617 | 511,300 | 10^{-1} | 3185 |
| 1400 | 4.98×10^{-12} | 302,944 | 509,873 | 1 | 3682 |
| 1600 | 1.18×10^{-9} | 273,506 | 507,978 | $\Delta_{\text{vap}} S^0(3682\text{K}) = 121.606 \pm 0.27$ (J·mol ⁻¹ ·K ⁻¹) | |
| 1800 | 8.12×10^{-8} | 244,337 | 505,535 | $\Delta_{\text{sub}} H^0(0\text{K}) = 511.00 \pm 1.00$ (kJ·mol ⁻¹) | |
| 2000 | 2.36×10^{-6} | 215,476 | 502,408 | | |
| 2100 | 9.91×10^{-6} | 201,174 | 500,519 | | |
| 2202(s) | 3.73×10^{-5} | 186,686 | 498,336 | | |
| 2202(l) | 3.73×10^{-5} | 186,686 | 477,336 | | |
| 2300 | 1.13×10^{-4} | 173,798 | 475,213 | | |
| 2400 | 3.17×10^{-4} | 160,740 | 473,058 | | |
| 2500 | 8.18×10^{-4} | 147,770 | 470,915 | | |
| 2600 | 1.95×10^{-3} | 134,886 | 468,789 | | |
| 2700 | 4.35×10^{-3} | 122,084 | 466,684 | | |
| 2800 | 9.12×10^{-3} | 109,359 | 464,603 | | |
| 2900 | 1.81×10^{-2} | 96,707 | 462,549 | | |
| 3000 | 3.43×10^{-2} | 84,126 | 460,525 | | |
| 3100 | 6.21×10^{-2} | 71,613 | 498,535 | | |
| 3200 | 0.108 | 59,163 | 456,581 | | |
| 3300 | 0.182 | 46,775 | 454,666 | | |
| 3400 | 0.296 | 34,443 | 452,793 | | |
| 3500 | 0.467 | 22,167 | 450,963 | | |
| 3600 | 0.717 | 9,941 | 449,179 | | |
| 3682 | 1.000 | 0 | 447,752 | | |
| 3700 | 1.076 | -2,239 | 447,443 | | |
| 3800 | 1.576 | -14,372 | 445,754 | | |

^a 1 atm = 101,325 Pa.^b ΔG^0 refers to $\Delta_{\text{sub}} G^0$ when $T < T_{\text{fus}}$ and $\Delta_{\text{vap}} G^0$ when $T > T_{\text{fus}}$ (and similarly for ΔH^0).

2.6. Vapor Pressure Data

Application of the third-law test to the vapor pressure measurements gave the enthalpies of sublimation at 298.15 K listed in Table VIII.

The values for ΔG^0 , P , and ΔH^0 reported in Table IX are calculated using $\Delta_{\text{sub}}H^0(298.15 \text{ K})$ and the Gibbs values for $V(s, l)$ and $V(g)$ from Table VI.

Most of the measurements for the thermodynamic properties have been carried out on the International Practical Temperature Scale of 1948 or 1958 (IPTS-48 or IPTS-58). It is worth noting that the effect of conversion of these properties to IPTS-68 is small and well within the uncertainty of these values.

ACKNOWLEDGMENTS

This work was supported by the Office of Standard Reference Data (OSRD) of the National Bureau of Standards (NBS), U.S. Department of Commerce, and the National Science Foundation. Part of the documentary activity essential to this work benefited from the comprehensive data base of the Thermophysical and Electronic Properties Information Analysis Center (TEPIAC), which is supported by the Defense Logistics Agency (DLA) of the U.S. Department of Defense.

The author wishes to express appreciation to Dr. John R. Rumble, Jr., of the NBS/OSRD for his guidance. The contribution of Dr. M. W. Chase for supplying thermodynamic properties of $V(g)$ is acknowledged. The assistance of Mr. Chad Poole in data extraction and thermodynamic calculations, Mrs. Vera Garcev in graphics, and Mrs. D. M. Lenartz in typing is also acknowledged.

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